G05DEF - NAG Fortran Library Routine Document

Note. Before using this routine, please read the Users' Note for your implementation to check the interpretation of bold italicised terms and other implementation-dependent details.

1 Purpose

G05DEF returns a pseudo-random real number taken from a log-normal distribution with parameters a and b.

2 Specification

real FUNCTION GO5DEF(A, B) real A, B

3 Description

The distribution has PDF (probability density function)

$$f(x) = \frac{1}{bx\sqrt{2\pi}} \exp\left(-\frac{(\ln x - a)^2}{2b^2}\right) \quad \text{if } x > 0,$$

$$f(x) = 0 \quad \text{otherwise}$$

i.e., $\ln x$ is normally distributed with mean a and standard deviation b. The routine returns the value $\exp y$, where y is generated by G05DDF from a Normal distribution with mean a and standard deviation b.

4 References

- [1] Knuth D E (1981) The Art of Computer Programming (Volume 2) Addison-Wesley (2nd Edition)
- [2] Kendall M G and Stuart A (1969) The Advanced Theory of Statistics (Volume 1) Griffin (3rd Edition)

5 Parameters

1: A — real

On entry: the mean a, of the distribution of $\ln x$.

2: B-real Input

On entry: the standard deviation b, of the distribution of $\ln x$. If B is negative, the distribution of the generated numbers – though not the actual sequence – is the same as if the absolute value of B were used.

6 Error Indicators and Warnings

None.

7 Accuracy

Not applicable.

8 Further Comments

None.

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9 Example

The example program prints the first five pseudo-random real numbers from a log-normal distribution with mean 1.0 and standard deviation 1.5, generated by G05DEF after initialisation by G05CBF.

The generator mechanism used is selected by an initial call to G05ZAF.

9.1 Program Text

Note. The listing of the example program presented below uses bold italicised terms to denote precision-dependent details. Please read the Users' Note for your implementation to check the interpretation of these terms. As explained in the Essential Introduction to this manual, the results produced may not be identical for all implementations.

```
GO5DEF Example Program Text
     NAG Fortran SMP Library, Release 2. NAG Copyright 2000.
      .. Parameters ..
      INTEGER
                       NOUT
     PARAMETER
                       (NOUT=6)
      .. Local Scalars ..
     DOUBLE PRECISION X
     INTEGER
                       Ι
      .. External Functions ..
     DOUBLE PRECISION GOSDEF
     EXTERNAL
                       G05DEF
      .. External Subroutines ..
     EXTERNAL
                      GO5CBF, GO5ZAF
      .. Executable Statements ..
     CALL GO5ZAF('0')
     WRITE (NOUT,*) 'GO5DEF Example Program Results'
     WRITE (NOUT,*)
     CALL GO5CBF(0)
     DO 20 I = 1, 5
         X = GO5DEF(1.0D0, 1.5D0)
         WRITE (NOUT, 99999) X
   20 CONTINUE
     STOP
99999 FORMAT (1X,F10.4)
     END
```

9.2 Program Data

None.

9.3 Program Results

```
G05DEF Example Program Results
6.0767
18.9017
29.0802
```

2.6121 26.4446

G05DEF.2 (last) [NP3445/2/pdf]